

Walking Talking - Solving Linear Equations

1.

(a) Solve $2x + 5 = 5(x + 1)$.

$$\begin{array}{rcl}
 2x + 5 & = & 5x + 5 \\
 \textcircled{-2x} & & \textcircled{-2x} \\
 5 & = & 3x + 5 \\
 \textcircled{-5} & & \textcircled{-5} \\
 0 & = & 3x \\
 0 & = & x
 \end{array}$$

[2]

(b) Solve $\frac{1}{3}(2x + 3) + 4x = 8$.

$$\begin{array}{rcl}
 \textcircled{\times 3} & & \textcircled{\times 3} \\
 2x + 3 + 12x & = & 24 \\
 14x + 3 & = & 24 \\
 \textcircled{-3} & & \textcircled{-3} \\
 14x & = & 21 \\
 \textcircled{\div 14} & & \textcircled{\div 14} \\
 x = \frac{21}{14} & = & 1\frac{7}{14} = 1\frac{1}{2}
 \end{array}$$

[3]

2.

(a) Solve $\frac{8x}{5} = 60$.

$(\times 5)$ $8x = 300$ $(\div 8)$

$8 \overline{) 300.0}$
 037.5

$(\div 8)$ $x = 37.5$

[2]

(b) Solve $\frac{3}{x} = 12$.

$(\times x)$ $3 = 12x$

$(\div 12)$ $x = \frac{3}{12} = \frac{1}{4}$

[1]

(c) Solve $9x - 4 = 7(x + 2)$.

$9x - 4 = 7x + 14$

$(-7x)$ $2x - 4 = 14$ (-14)

$(+4)$ $2x = 18$ $(\div 2)$

$(\div 2)$ $x = 9$

[3]

(d) Solve the inequality $10x + 5 > 45$.

(-5) $10x > 40$ $(\div 10)$

$(\div 10)$ $x > 4$

[2]

(e) Write down the smallest whole number that satisfies the inequality $9x > 60$.

$9x > 60$
 $(\div 9)$ $x > \frac{60}{9}$

$x > 6\frac{2}{3}$

$x > 6\frac{2}{3}$

so the smallest whole number is 7

[2]

3.

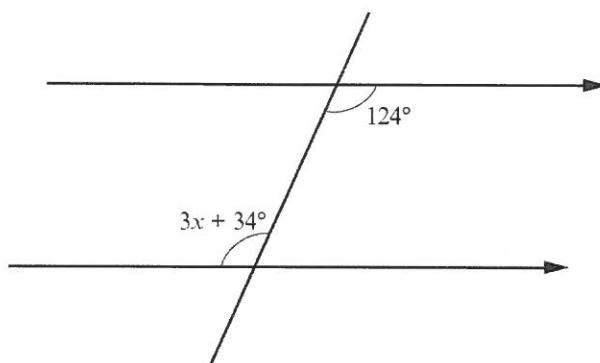


Diagram not drawn to scale

Use the information in the diagram above to find the value of x .

[3]

$$\begin{array}{rcl}
 3x + 34 & = & 124 \\
 \textcircled{-34} & & \textcircled{-34} \\
 3x & = & 90 \\
 \textcircled{\div 3} & & \textcircled{\div 3} \\
 x & = & 30 \\
 x & = & 30^\circ
 \end{array}$$

4.

Solve $\frac{8x-5}{3} + \frac{4x+5}{4} = \frac{149}{12}$.

$$\begin{array}{rcl}
 \textcircled{\times 12} & & \textcircled{\times 12} \\
 \frac{12(8x-5)}{3} + \frac{12(4x+5)}{4} = \frac{12(149)}{12} & \rightarrow & 4(8x-5) + 3(4x+5) = 149 \\
 32x - 20 + 12x + 15 & = & 149 \\
 44x - 5 & = & 149 \\
 \textcircled{+5} & & \textcircled{+5} \\
 44x & = & 154 \\
 \textcircled{\div 44} & & \textcircled{\div 44} \\
 x & = & \frac{154}{44} = \frac{77}{22} = \frac{7}{2}
 \end{array}$$

[4]

5.

(a) Solve $\frac{3x}{4} = 24$. $3x = 96$
 $x = 32$

$3x = 96$ $\div 3$

$x = 32$ $\div 3$

[2]

(b) Solve $\frac{8}{x} = 16$. $8 = 16x$

$8 = 16x$ $\div 16$

$\frac{1}{2} = \frac{8}{16} = x$ $\div 16$

[1]

(c) Solve $7(5x - 4) = 77$.

$35x - 28 = 77$

$35x = 105$ $+28$

$x = \frac{105}{35} = \frac{21}{7} = 3$ $\div 35$

[3]

(d) Solve the inequality $6x + 5 < 47$.

$6x < 42$ -5

$x < 7$ $\div 6$

[2]

(e) Write down the smallest whole number that satisfies the inequality $3x > 67$.

$x > \frac{67}{3}$ $\div 3$

$x > 22\frac{1}{3}$ $\div 3$

smallest whole number is 23

[2]

6.

$ABCD$ is a parallelogram. All the angles are measured in degrees.

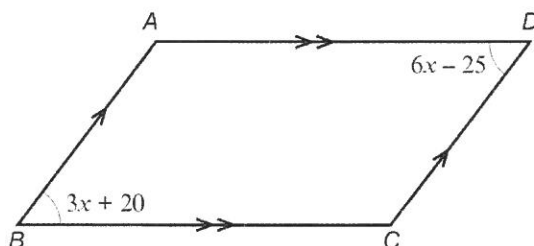


Diagram not drawn to scale

Find the size of \hat{BCD} .

[5]

$$6x - 25 = 3x + 20$$

$$(-3x)$$

$$(-3x)$$

$$3x - 25 = 20$$

$$(+25)$$

$$(+25)$$

$$3x = 45$$

$$(\div 3)$$

$$(\div 3)$$

$$x = 15$$

$$\begin{aligned} \text{So } \hat{CDA} &= 6(15) - 25 \\ &= 90 - 25 \\ &= 65^\circ \end{aligned}$$

$$\therefore \hat{BCA} = 180 - 65 = 115^\circ$$

7.

(a) Solve $8x - 11 = 3x + 29$.

$(-3x)$

$(-3x)$

$$5x - 11 = 29$$

$(+11)$

$$5x = 40$$

$(+11)$

$(\div 5)$

$(\div 5)$

$$x = 8$$

[3]

(b) Factorise $7x + 49$.

$$7(x+7)$$

[1]

(c) Factorise $x^2 - 10x$.

$$x(x-10)$$

[1]

(d) Expand $2x(x+6)$.

$$2x^2 + 12x$$

[2]

8.

(a) Simplify $3g + 5g - 6g$.

[1]

$2g$

(b) Find the value of $7x - 4y$ when $x = 5$ and $y = 6$.

[2]

$$7(5) - 4(6) = 35 - 24 = 11$$

(c) Solve

(i) $6x = 24$,

[1]

$\div 6$

$\div 6$

$$x = 4$$

(ii) $x - 7 = 29$.

[1]

$+7$

$+7$

$$x = 36$$

9.

Solve the following equation.

[3]

$$\frac{5x-1}{2} - x = \frac{1}{2}$$

(x2)

$$5x-1-2x=1$$

(x2)

$$3x-1=1$$

(+1)

(+1)

$$3x=2$$

(:3)

(:3)

$$x = \frac{2}{3}$$

10.

Yellow, blue and green tickets are sold in a raffle to raise money for charity.

The probability of the winning ticket being a particular colour is given in the following table.

Colour of ticket	Yellow	Blue	Green
Probability	$2a$	0.4	$3a$

Find the probability that the winning ticket is green.

[3]

$$2a + 0.4 + 3a = 1$$

$$5a + 0.4 = 1$$

(-0.4)

(-0.4)

$$5a = 0.6$$

$$\text{green} = 3(0.12)$$

$$= 3 \times 0.12$$

(:5)

(:5)

$$= 0.36$$

$$a = 0.12$$

$$\begin{array}{r} 0.12 \\ 5 \overline{)0.60} \end{array}$$